

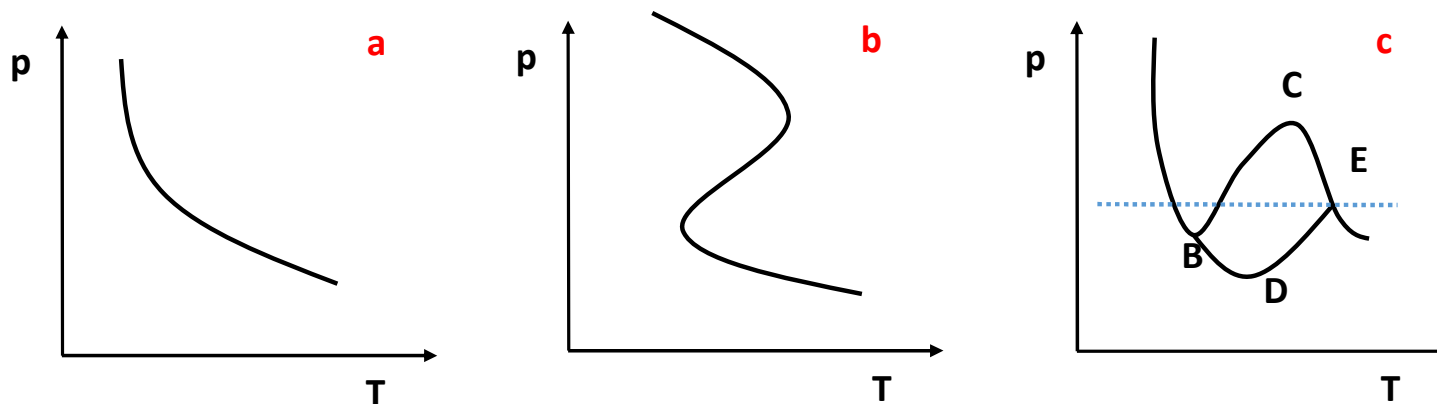


Aerospace Combustion

Lecture 6:

Short Introduction to Chemical Kinetics

How Does it Burn ?



Pressure - temperature diagrams for different types of reactions:

- a) Thermal feedback solely
- b) Chain branching-thermal interaction typical for hydrogen oxidation
- c) Chain branching-thermal interaction typical for alkane oxidation

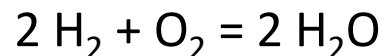
The answer requires a detailed chemical kinetics mechanism.



Chemistry is Complex (even for simple molecular reactions)

Let's look at the reaction of hydrogen and oxygen, a gas mixture which is highly explosive. It can be described with 1 global reaction.

Stoichiometric global reaction equation:



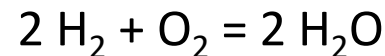
This chain-branching reaction is highly exothermic; but mixtures of gaseous hydrogen and oxygen are quite stable at atmospheric conditions. Any conceivable direct reaction between the two gases is zero. In fact, the reaction half time at atmospheric conditions is estimated to be larger than the age of the universe.

But, if the reaction is initiated by some free-radical species, the reaction proceeds extremely rapid and violent and in some cases even explosive.



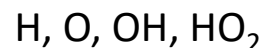
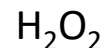
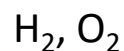
Chemistry is Complex

Let's stick to the reaction of hydrogen and oxygen

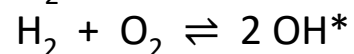
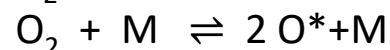
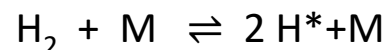


Species

- Reactants
- Intermediates,
- Radicals
- Products

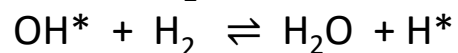
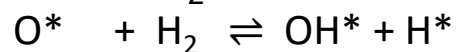
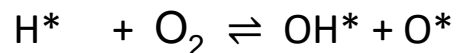


Chain Initiation Reactions (Generation of Radicals)



M can either be a molecule which collides with the reactants to initiate the radical formation or an atom of a hot surface.

Chain Propagation Reactions (Generation of Radicals)



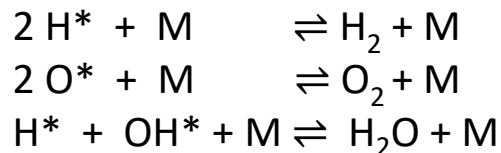
Branching reactions

Extension reaction



Chemistry is Complex

Chain Termination Reactions (Consumption of Radicals)

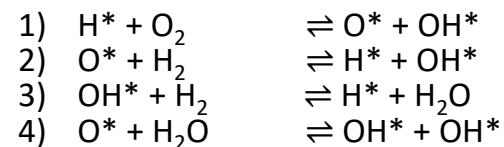


A well-developed mechanism describes correctly the balance between the chain extension rate and the chain termination rate.

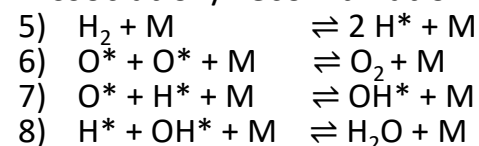
That is provided with the complete **reaction pool (particle zoo)** (a generation and a consumption of components, heat release) and the correct **rate constants** of reactions.

H₂/O₂ Reactions

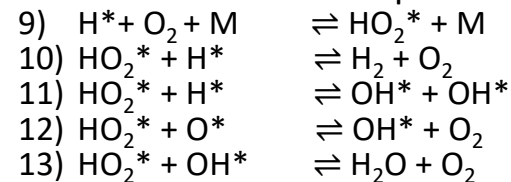
Chain Reactions



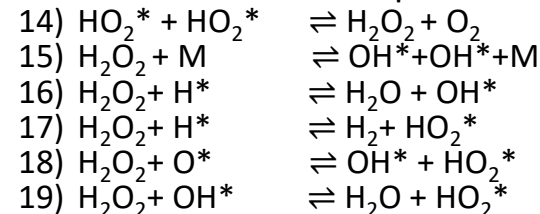
Dissociation/Recombination



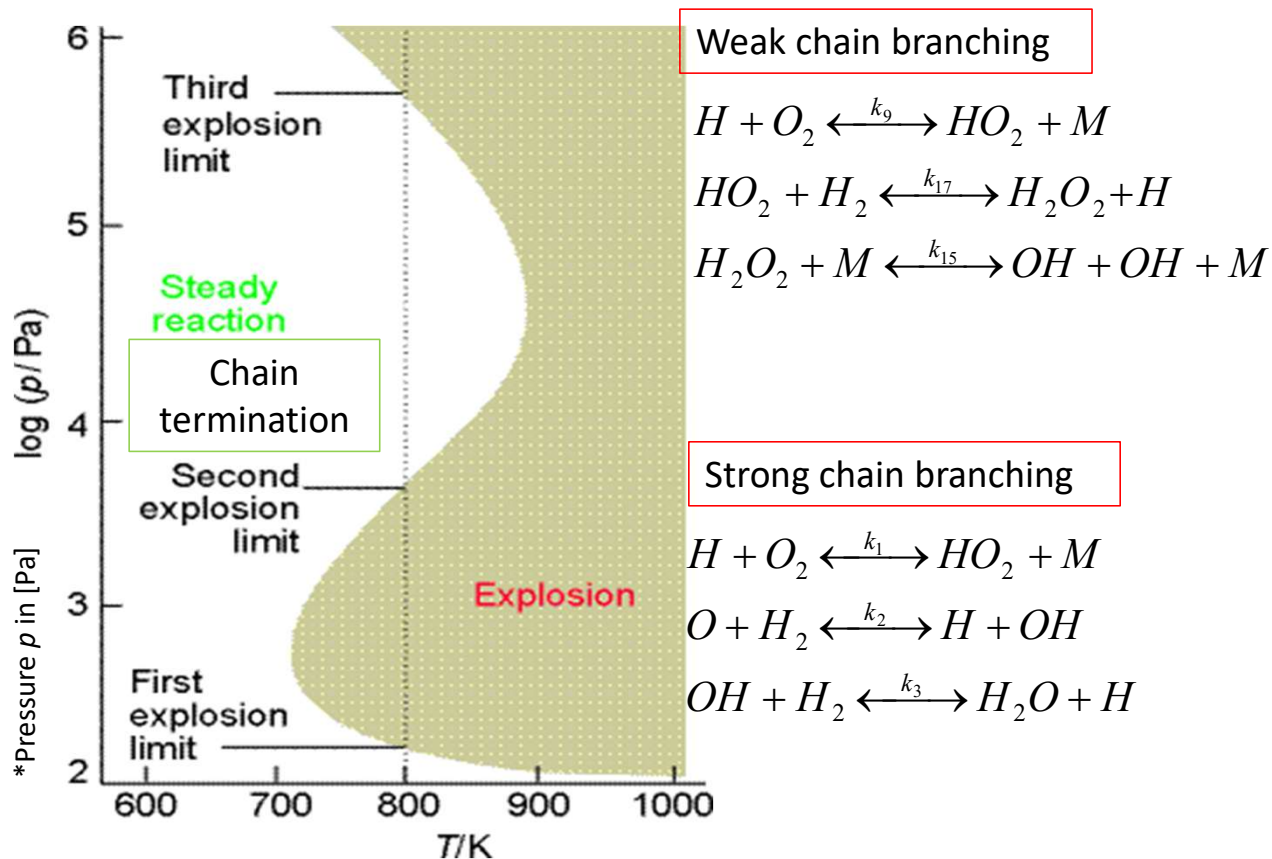
Formation and Consumption of HO₂^{*}



Formation and Consumption of H₂O₂



H₂ – O₂ Chemistry (Homogeneous Ignition)



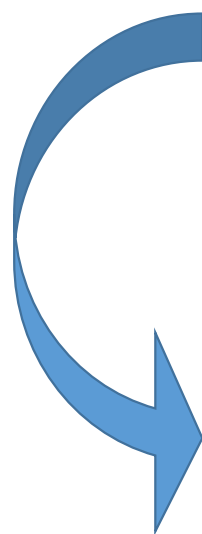
Species:

H₂, O₂, H₂O, (Major species);
 H, O, OH, HO₂, H₂O₂ (Radicals)

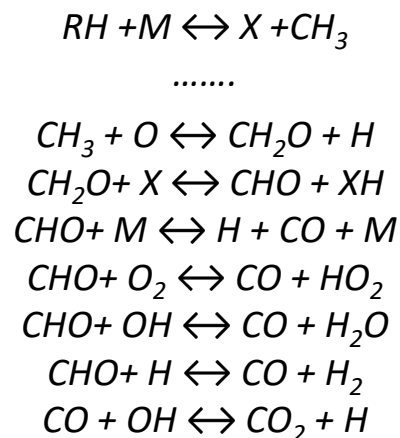
Light Hydrocarbon Oxidation: General Scheme

In a very simplistic point-of-view, hydrocarbon combustion (related to number of C atom) can be seen as a two-step process:

- a) breakdown of fuel into CO
- b) oxidation of CO to CO₂.



Small chemistry

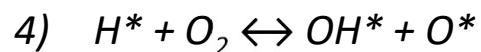
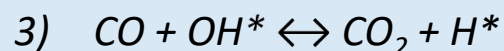
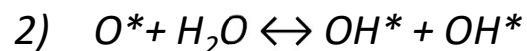
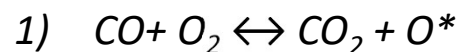




Light Hydrocarbon Oxidation: CO Oxidation

CO Oxidation is a very slow process in absence of even small amounts of H_2 or H_2O

In case of H_2O as the primary hydrogen-containing species, CO oxidation can be described by

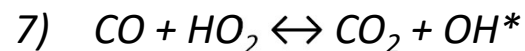
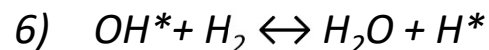
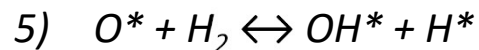


1) Is slow; not sufficient contribution to CO_2 formation, but chain initiation reaction

3) is the actual CO oxidation step; also chain propagation step producing H radicals

2) and 4) are chain-branching reactions producing OH and $OH + O$

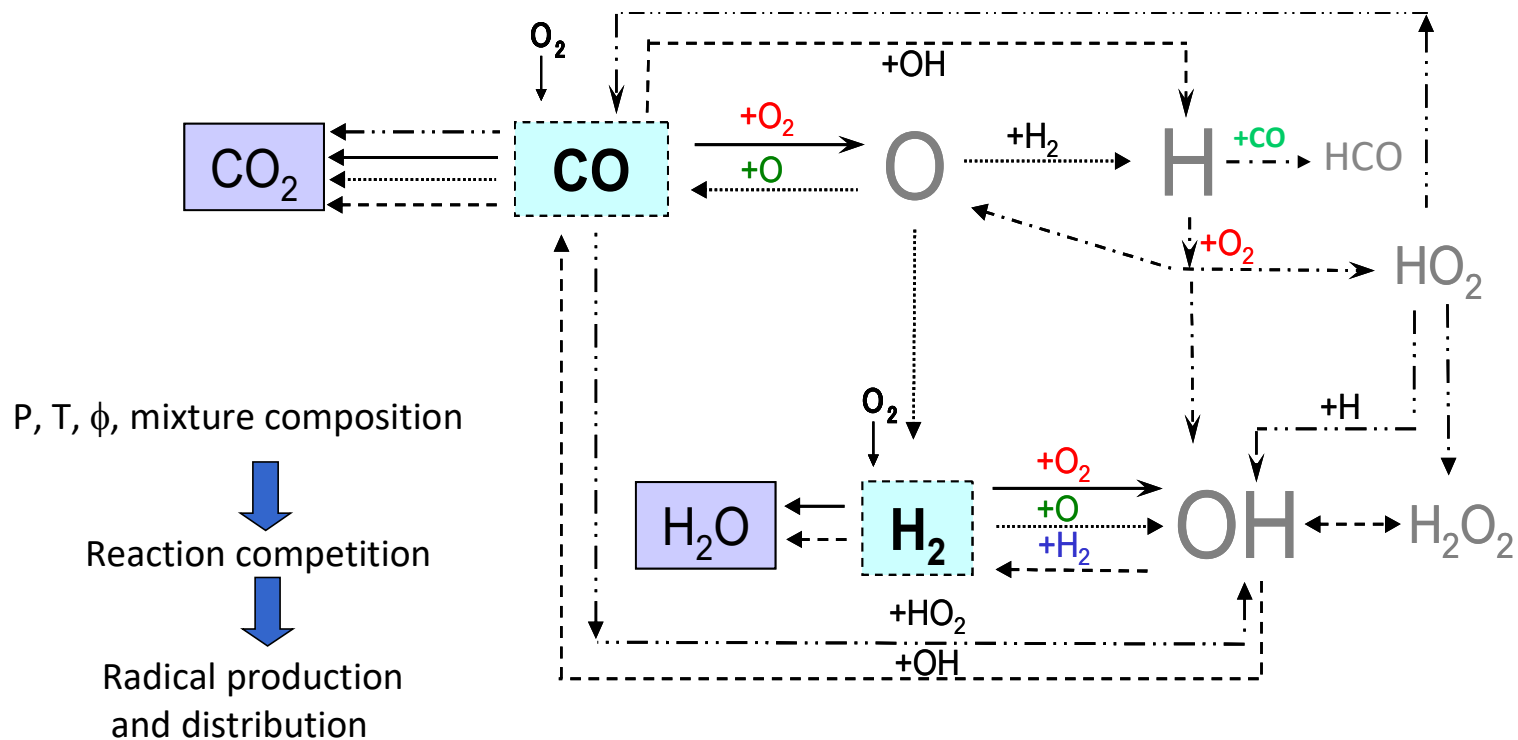
In the presence of H_2 , the following reactions are involved:



If H_2 is present, the entire H_2-O_2 reaction system should be included to describe CO oxidation

Principle Scheme of Radical Production

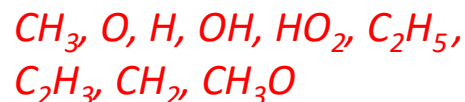
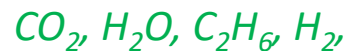
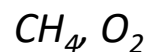
$H_2 + CO$ chemistry



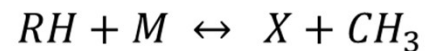
Methane Combustion

Species

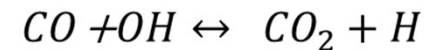
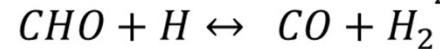
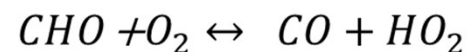
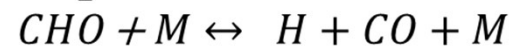
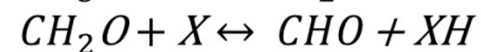
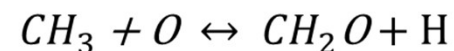
- Input species, reactants
- products
- intermediates
- radicals



Chain-initiation

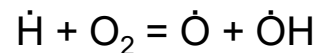
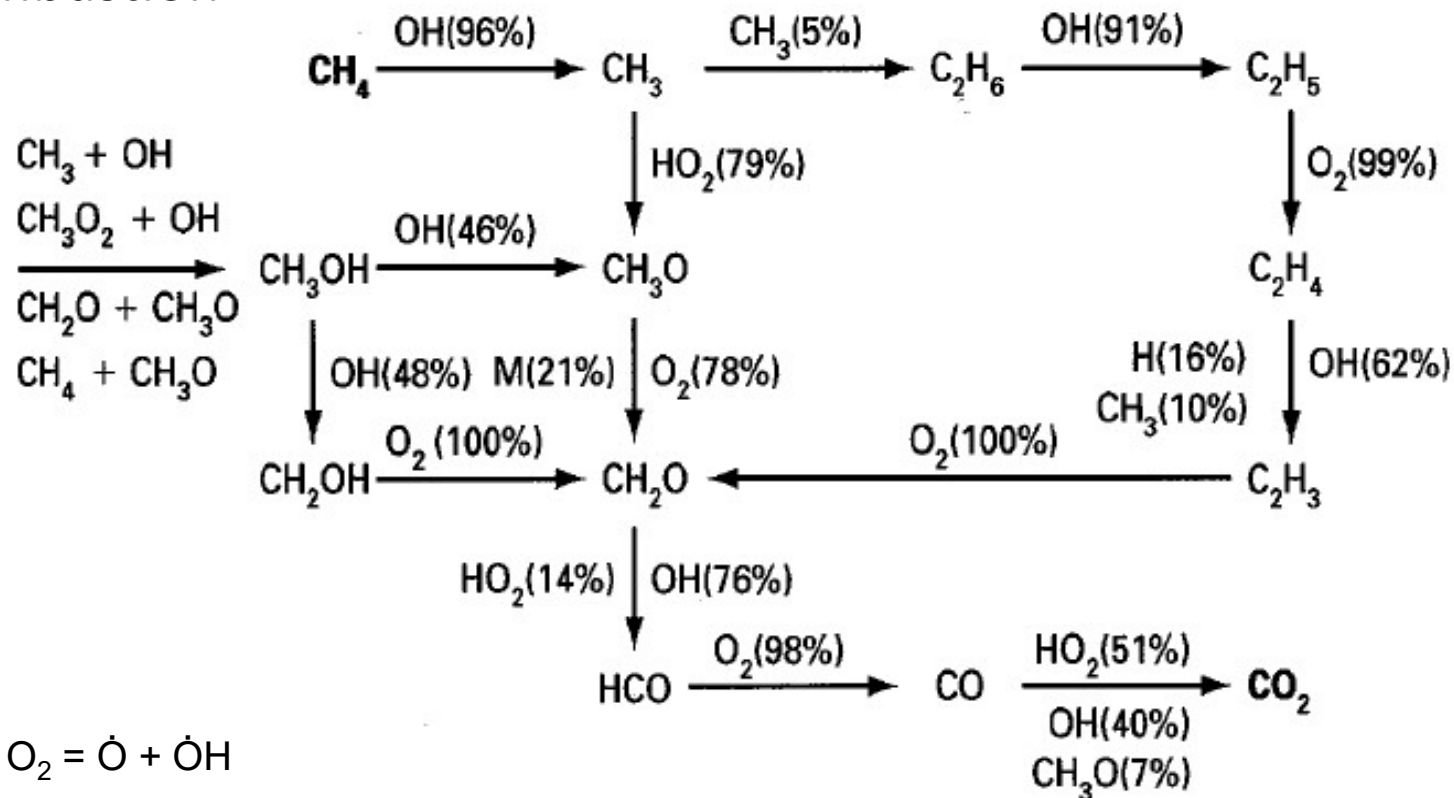


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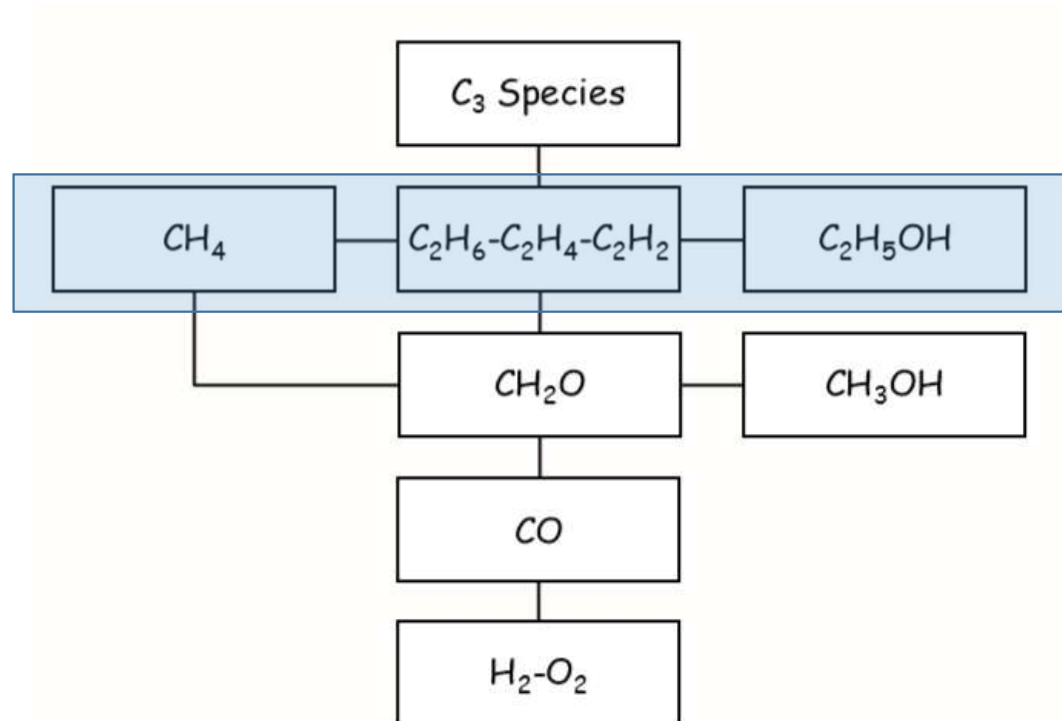
H₂ + CO chemistry

Methane Combustion



$$k = 1.04 \times 10^{14} \exp(-15286/RT) \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$$

Oxidation of Higher Alkanes



FUEL

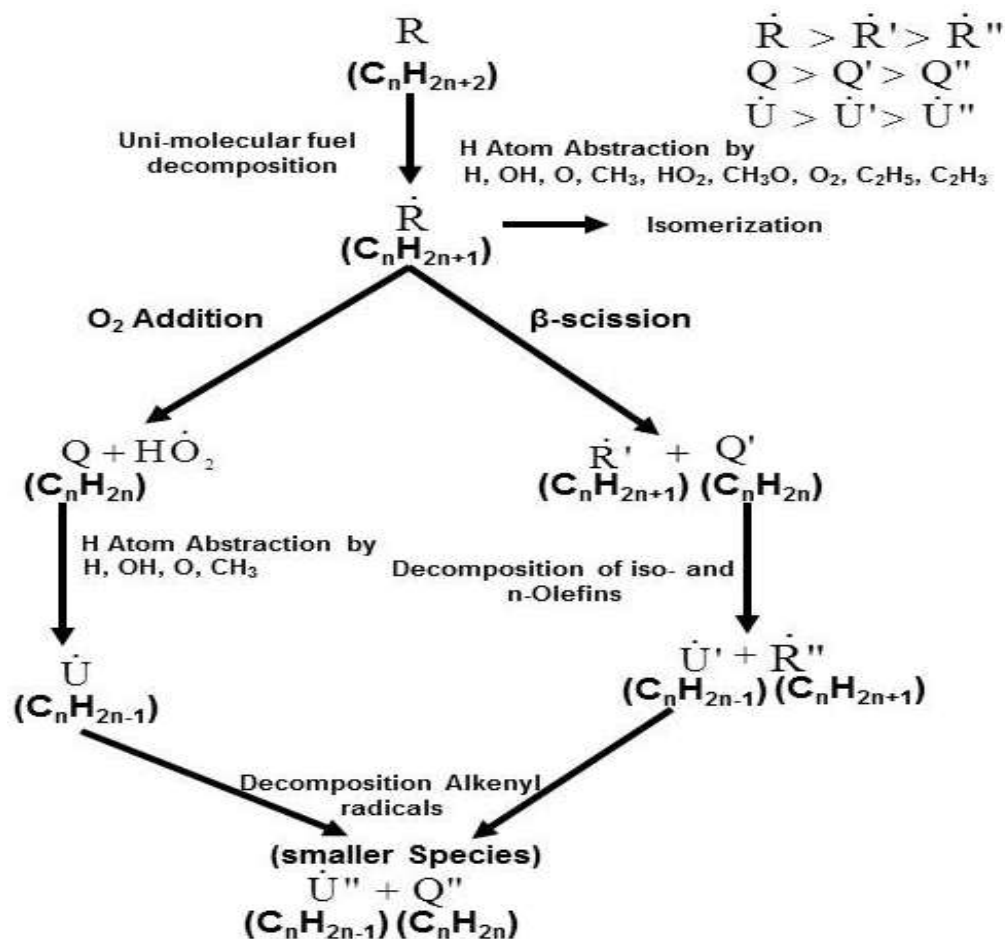


CH_3 , relatively unreactive, and C_2H_5 , relatively reactive

Long Alkanes Oxidation

High Temperature Route

Main Reaction Paths





Long Alkanes Oxidation



Reaction mechanism		$k = A T^n \exp(-E_a/RT)$						C^3
Reaction		A_f	n_f	E_{a_f}	A_r	n_r	E_{a_r}	
c2h5oh	= c2h4+h2o	1.25E+14	0.1	2.00E+04	1.11E+07	1.77	8.08E+03	
c2h5oh	= ch2oh+ch3	2.00E+23	-1.68	9.64E+04	8.38E+14	-0.22	7.02E+03	
c2h5oh	= c2h5+oh	2.40E+23	-1.62	9.95E+04	9.00E+15	-0.24	4.65E+03	
c2h5oh	= ch3cho+h2	7.24E+11	0.1	9.10E+04	4.91E+07	0.99	7.50E+04	
c2h5oh+o2	= pc2h4oh+ho2	2.00E+13	0	5.28E+04	2.19E+10	0.28	4.43E+02	
c2h5oh+o2	= sc2h4oh+ho2	1.50E+13	0	5.02E+04	1.95E+11	0.09	4.88E+03	
c2h5oh+oh	= pc2h4oh+h2o	1.81E+11	0.4	7.17E+02	4.02E+08	0.92	1.79E+04	
c2h5oh+oh	= sc2h4oh+h2o	6.18E+10	0.5	3.80E+02	1.63E+09	0.83	2.39E+04	
c2h5oh+oh	= c2h5o+h2o	1.50E+10	0.8	2.53E+03	7.34E+09	0.91	1.72E+04	
c2h5oh+h	= pc2h4oh+h2	1.88E+03	3.2	7.15E+03	3.93E-01	3.83	9.48E+03	
c2h5oh+h	= sc2h4oh+h2	8.95E+04	2.53	3.42E+03	2.21E+02	2.97	1.28E+04	
c2h5oh+h	= c2h5o+h2	5.36E+04	2.53	4.41E+03	2.47E+03	2.74	4.19E+03	
c2h5oh+ho2	= pc2h4oh+h2o2	2.38E+04	2.55	1.65E+04	2.88E+03	2.48	2.83E+03	
c2h5oh+ho2	= sc2h4oh+h2o2	6.00E+12	0	1.60E+04	8.59E+12	-0.26	9.42E+03	
c2h5oh+ho2	= c2h5o+h2o2	2.50E+12	0	2.40E+04	6.66E+13	-0.48	7.78E+03	





Reaction Rate Coefficients

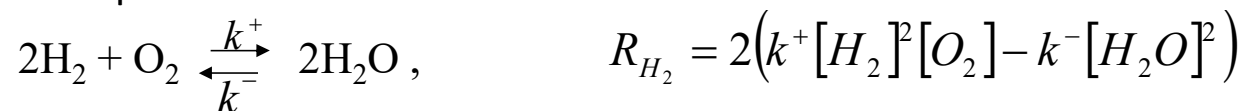
Rate of production (consumption) of species i in process

$$\frac{dC_i}{dt} = \sum_{j=1}^S R_{ij} \quad \Leftrightarrow \quad R_i = \sum_j R_{ij} = \sum_j \nu_{ij} w_j$$

$$w_j = \left(k_j^+ \prod_{i=1}^N [c_i]^{v_{ij}^+} - k_j^- \prod_{i=1}^N [c_i]^{v_{ij}^-} \right) \quad \text{- rate of reaction } j$$

$$k_j(T) = A_j T^{n_j} \exp(-E_{a,j} / RT) \quad \text{- coefficient of rate of reaction } j, \text{ Arrhenius form}$$

Example :



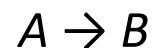


Reaction Rate Coefficients

$$\frac{d(C)}{dt} \sim k[C]^{\nu} \Rightarrow k \sim 1/([C]^{\nu-1} \cdot t)$$

$$[X] = \frac{N \text{ molecules / mole}}{V} \Rightarrow [k] \sim \left(\frac{V}{\text{mole}} \right)^{\nu-1} \frac{1}{c}$$

One body reaction



$$\nu = 1$$

$$[k_I] = [t^{-1}] = [s^{-1}]$$

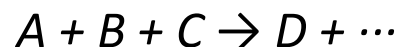
Two bodies reaction



$$\nu = 2$$

$$[k_{II}] = \left[\frac{cm^3}{mol \cdot s} \right]$$

Three bodies reaction

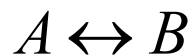
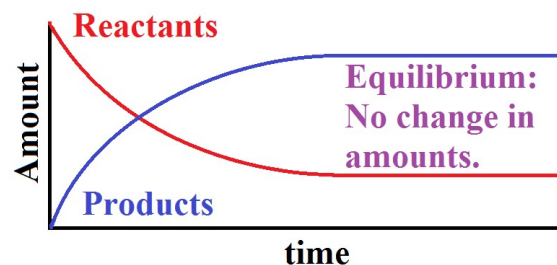
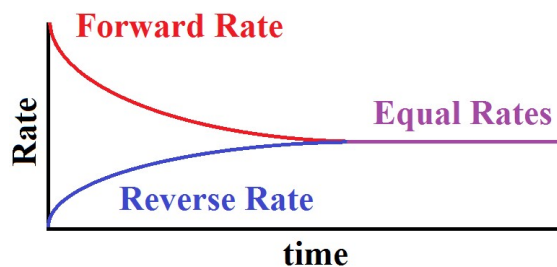


$$\nu = 3$$

$$[k_{III}] = \left[\frac{cm^6}{mol^2 \cdot s} \right]$$

Chemical Equilibrium

$$\sum_{k=1}^K \nu_{ki}^+ \chi_k = \sum_{k=1}^K \nu_{ki}^- \chi_k \quad \Rightarrow \quad k_{fi} \prod_{k=1}^K [X_k]^{\nu'_{ki}} = k_{ri} \prod_{k=1}^K [X_k]^{\nu''_{ki}}$$



$$K_p = \exp(-\Delta G_T^0 / RT)$$

$$\frac{k_{fi}}{k_{ri}} = \frac{\prod_{k=1}^K [X_k]^{\nu''_{ki}}}{\prod_{k=1}^K [X_k]^{\nu'_{ki}}} = K_p$$

Thermodynamic Equilibrium which can be reached through chemical reactions is Chemical Equilibrium

$$\Delta G_T^0 = \Delta H^0 - T\Delta S^0$$

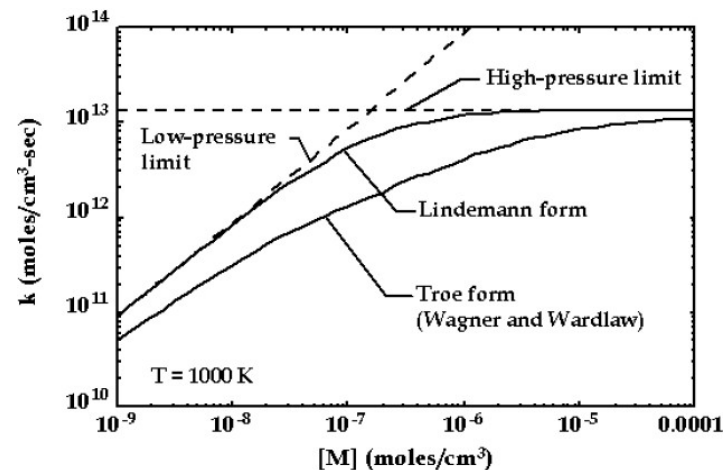
Pressure Dependent Reactions

Mono-molecular re-combination (Fall-off Reactions)

Example: Recombination reaction of methyl radicals

At high pressures we have a direct recombination reaction $\text{CH}_3 + \text{CH}_3 = \text{C}_2\text{H}_6$

At low pressures a third body collision is necessary to provide the activation energy $\text{CH}_3 + \text{CH}_3 + \text{M} = \text{C}_2\text{H}_6 + \text{M}$



Lindemann approximation
 (assumes $F = 1$)

high pressure rate: $k_0 = A_0 T^{\beta_0} \exp(-E_0 / R_c T)$

low pressure rate: $k_\infty = A_\infty T^{\beta_\infty} \exp(-E_\infty / R_c T)$

any pressure: $k = k_\infty \left(\frac{p_r}{1 + p_r} \right) F$; $p_r = \frac{k_0 [M]}{k_\infty}$

Troe approximation

$$\log F = \left[1 + \left\{ \frac{\log p_r + c}{n - 0.14(\log p_r + c)} \right\}^2 \right]^{-1} \log F_{cent}$$

$$c = -0.4 - 0.67 \log F_{cent} \quad n = 0.75 - 1.27 \log F_{cent}$$

$$F_{cent} = (1 - \alpha) \exp(-T / T^{***}) + \alpha \exp(-T / T^{**}) + \exp(-T^{**} / T)$$

Pressure Dependent Reactions

Chemically activated bimolecular reactions with a rate coefficient described as

$$k = k_0 \left(\frac{p_r}{1 + p_r} \right) F;$$

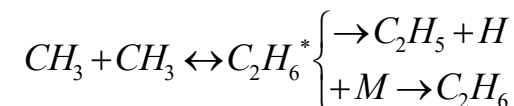
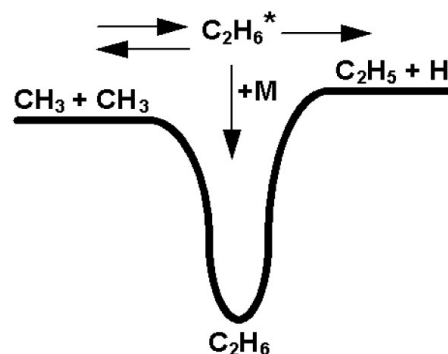
Example: Reaction of methyl radicals to form ethyl and hydrogen radicals which goes through activated ethane similarly as the previously discussed low pressure recombination reaction

With increasing pressure, deactivation collisions of activated ethane increase the rate of ethane formation while in parallel precluding dissociation to ethane and hydrogen radicals thus decrease this rate coefficient.

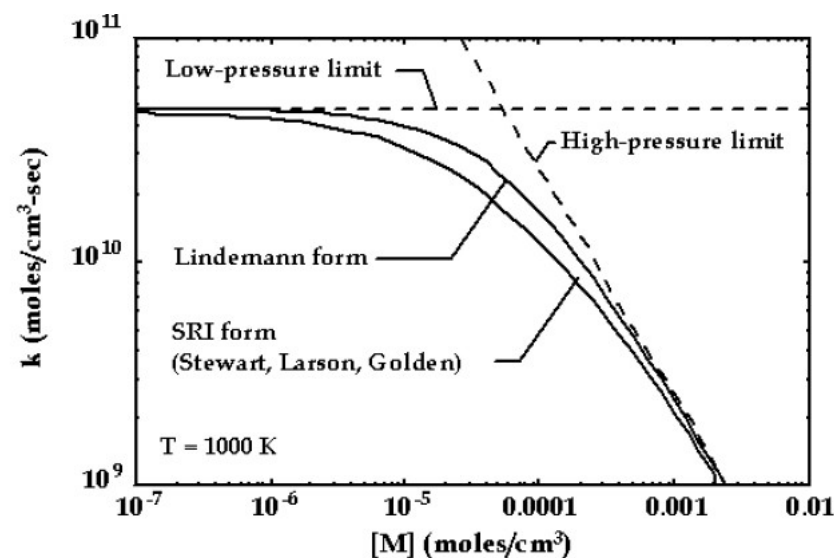
SRI approximation:

$$F = d \left[a \exp\left(\frac{-b}{T}\right) + \exp\left(\frac{-T}{c}\right) \right]^X T^e$$

$$X = \frac{1}{1 + (\log p_r)^2}$$



two competing reaction channels





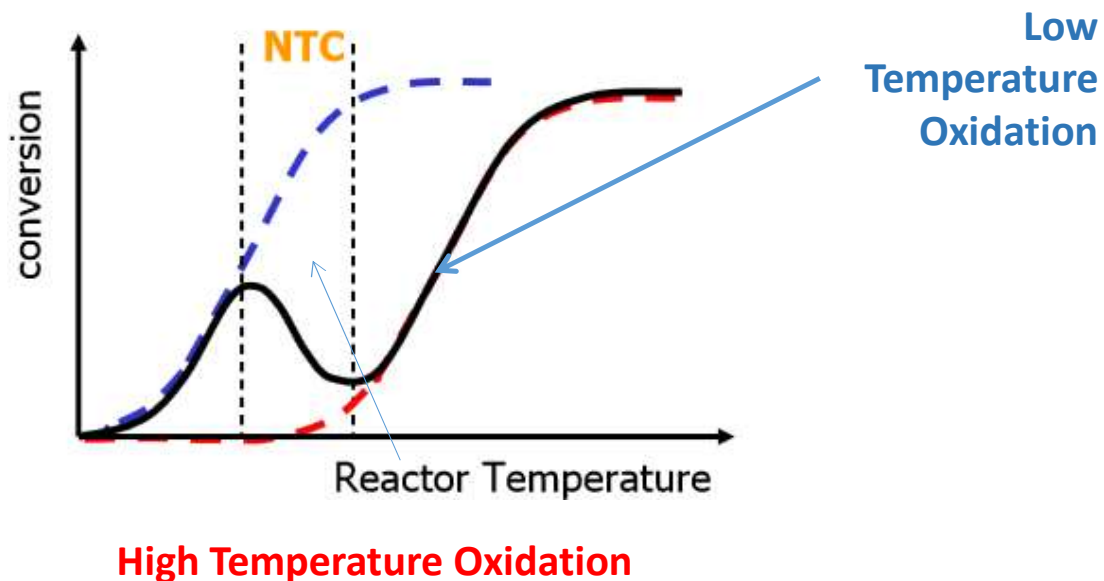
Pressure Dependent Reactions

For both pressure dependent reactions, the factor F is an empirical correction coefficient which accounts for various effects of energy transfer efficiency by collisions of molecules. These include

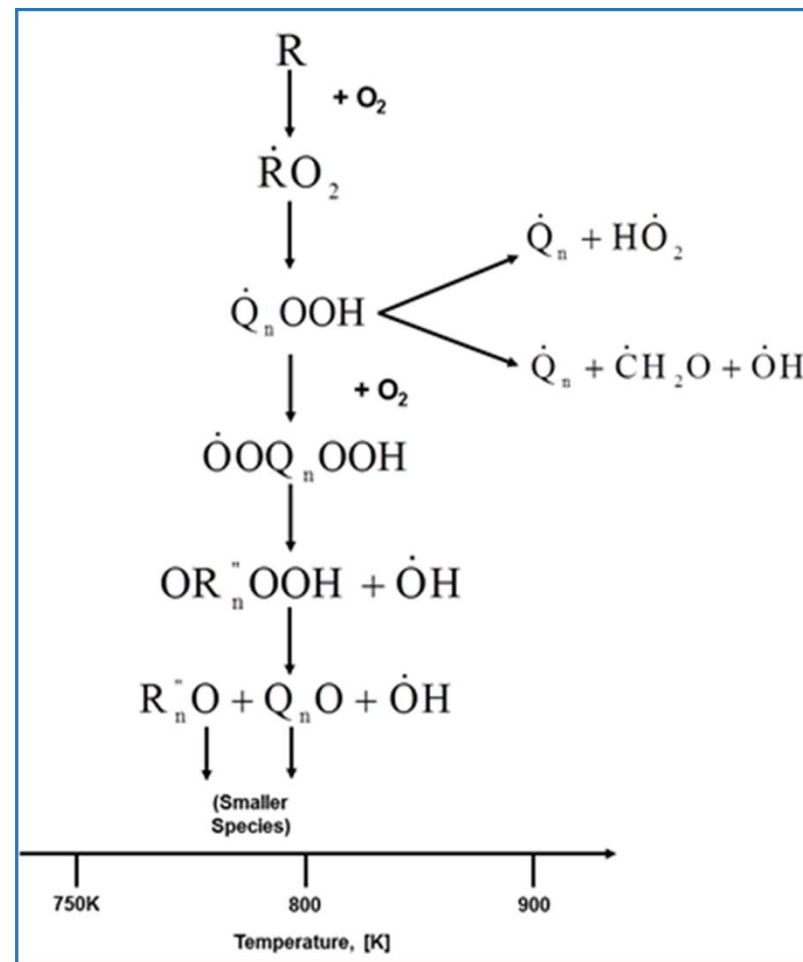
- losses of vibrational energy due to anharmonicity of the potential,
- losses of vibrational modes for certain reactions
- energy dependency of the density of vibrational states
- rotational energies which aren't taken into account in the simple approximation,
- reduction of this correction factor in cases where centrifugal barriers are present
- presence of internal rotors

Specifics of Long Alkanes

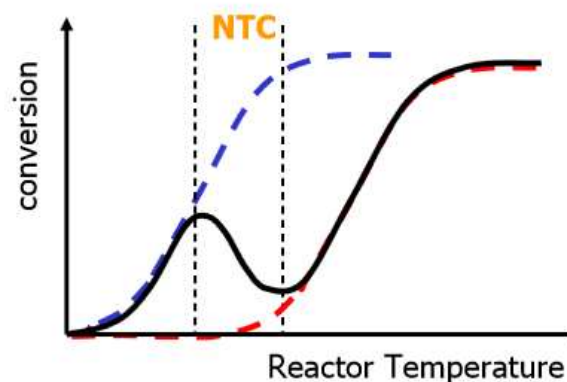
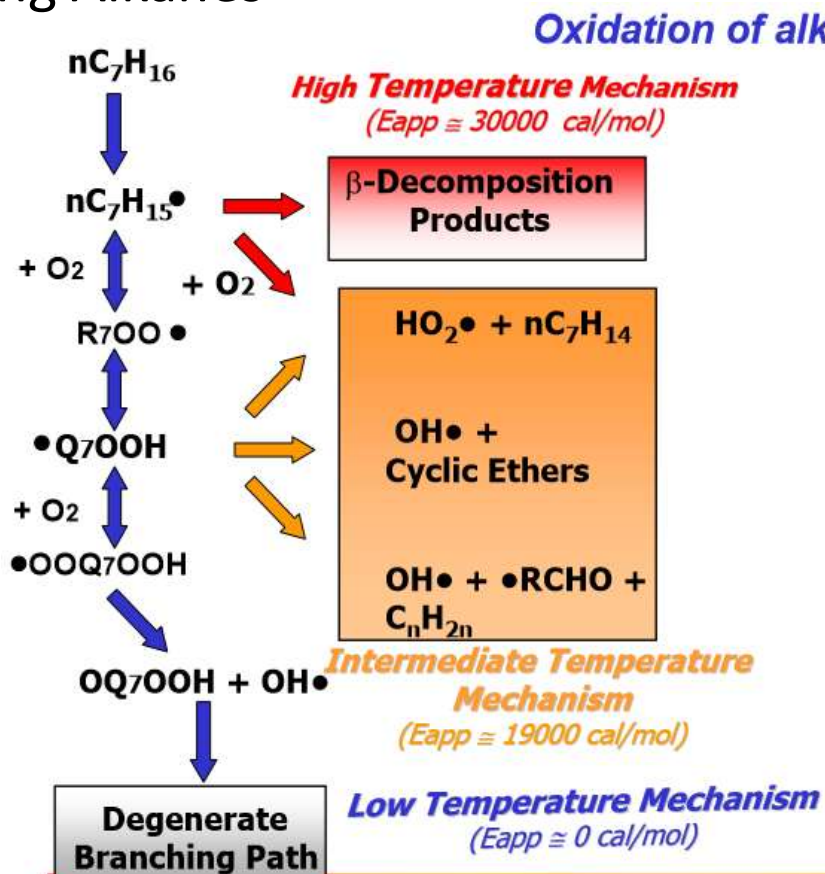
H/C with $n > 3$ have negative temperature region (NTC)
 (ignition delay increases with increasing temperature)



Fuel Decomposition through reactions of the type 1) – 8)



Specifics of Long Alkanes



SAFEKINEX WORKSHOP: Theoretical background: Detailed oxidation kinetics

By courtesy of T. Faravelli

F. Battin-Leclerc

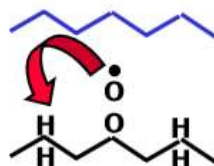
Specifics of Long Alkanes

Generally, isomers have a substantially lower reactivity (i.e. i-octane to avoid knock)

i-octane = -C₈H₁₈ = 2,2,4-trimethyl-pentane (5 carbon atoms with 2 methyl groups sitting on the 2nd C atom and a third one on the 4th .)

Difference between linear and branched alkanes

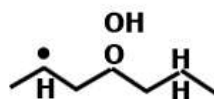
n-heptane High reactivity



Peroxy radicals

4 secondary H atoms
Isomerization (1-5):
six membered ring

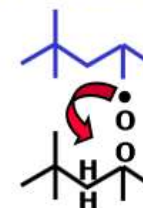
$$k = 4 \times 10^{11.0} \exp(-20000/RT) \text{ [s}^{-1}\text{]}$$



Alkyl-hydroperoxy radicals

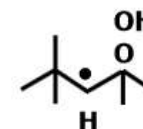
$$k(700) = 10^{5.4} \text{ [s}^{-1}\text{]}$$

iso-octane Low reactivity



2 secondary H atoms
Isomerization (1-4):
five membered ring

$$k = 2 \times 10^{11.8} \exp(-26000/RT) \text{ [s}^{-1}\text{]}$$



$$k(700) = 10^{4.0} \text{ [s}^{-1}\text{]}$$

By courtesy of T. Faravelli

SAFEKINEX WORKSHOP: Theoretical background: Detailed oxidation kinetics

F. Battin-Leclerc



These very different reactions yield very large detailed chemical kinetic schemes which aren't suited to be implemented in CFD tools to handle combustion problems.

As long as temperatures in the system are high enough chemical equilibrium may be assumed and then the situation can be treated such that you use a library of previously calculated equilibrium compositions depending on pressure, temperature and initial mixture composition (flamelet approach).

In case of low temperatures you normally can't assume equilibrium anymore and you have to apply a so-called finite-rate chemistry approach and this requires a chemical mechanisms sufficiently small (typically < 20 reactions).

How do we come to reliable reduced kinetic mechanisms ?



What you should remember



- Explosive limits of H₂/O₂ mixtures
- General reaction mechanism (initiation, propagation and termination)
- Difference between light hydrocarbon (methane) and heavy hydrocarbon reactions
- NTC region for higher alkane combustion and its explanation
- What kind of pressure dependent reactions do you know ?
- What can you say about reaction rate and production rate at chemical equilibrium ?



Mechanism for Ammonium-perchlorate Decomposition

		Arrhenius parameters			
		A	b	Ea	
1)	HClO_4	$\rightleftharpoons \text{ClO}_3^* + \text{OH}^*$	1.0 e14	0.0	39100
2)	$\text{HClO}_4 + \text{HNO}$	$\rightleftharpoons \text{ClO}_3^* + \text{H}_2\text{O} + \text{NO}^*$	1.5 e13	0.0	6000
3)	ClO_3^*	$\rightleftharpoons \text{ClO}^* + \text{O}_2$	1.7 e13	0.5	0.0
4)	$\text{Cl}_2 + \text{O}_2 + \text{M}$	$\rightleftharpoons \text{ClO}_2^* + \text{Cl}^* + \text{M}^*$	6.0 e08	0.0	1200
5)	$\text{ClO}^* + \text{NO}^*$	$\rightleftharpoons \text{Cl}^* + \text{NO}_2^*$	6.78 e12	0.0	311
6)	$\text{ClO}^* + \text{ClOH}$	$\rightleftharpoons \text{Cl}_2 + \text{HO}_2^*$	1.0 e11	0.0	10000
7)	$\text{ClOH} + \text{OH}^*$	$\rightleftharpoons \text{ClO}^* + \text{H}_2\text{O}$	1.8 e13	0.0	0
8)	$\text{HCl} + \text{OH}^*$	$\rightleftharpoons \text{Cl}^* + \text{H}_2\text{O}$	5.0 e11	0.0	750
9)	$\text{Cl}_2 + \text{H}^*$	$\rightleftharpoons \text{HCl} + \text{Cl}^*$	8.4 e13	0.0	1150
10)	$\text{ClO}^* + \text{NH}_3$	$\rightleftharpoons \text{ClOH} + \text{NH}_2^*$	6.0 e11	0.5	6400
11)	$\text{NH}_3 + \text{Cl}^*$	$\rightleftharpoons \text{NH}_2^* + \text{HCl}$	4.5 e11	0.5	100
12)	$\text{NH}_3 + \text{OH}^*$	$\rightleftharpoons \text{NH}_2^* + \text{H}_2\text{O}$	5.0 e07	1.6	955
13)	$\text{NH}_2^* + \text{O}_2$	$\rightleftharpoons \text{HNO} + \text{OH}^*$	3.0 e09	0.0	0
14)	$\text{NH}_2^* + \text{NO}^*$	$\rightleftharpoons \text{H}_2\text{O} + \text{N}_2$	6.2 e15	-1.3	0
15)	$\text{HNO} + \text{OH}^*$	$\rightleftharpoons \text{NO}^* + \text{H}_2\text{O}$	1.3 e07	1.9	-950
16)	$\text{HNO} + \text{O}_2$	$\rightleftharpoons \text{NO}_2^* + \text{OH}^*$	1.5 e13	0.0	10000
17)	$\text{HNO} + \text{H}^*$	$\rightleftharpoons \text{H}_2 + \text{NO}^*$	4.5 e11	0.7	660
18)	$\text{NO}^* + \text{H}^* + \text{M}$	$\rightleftharpoons \text{HNO} + \text{M}$	8.9 e19	-1.3	740
19)	$\text{HO}_2^* + \text{N}_2$	$\rightleftharpoons \text{HNO} + \text{OH}^*$	2.7 e10	0.5	41800
20)	$\text{NO}^* + \text{HO}_2^*$	$\rightleftharpoons \text{NO}_2^* + \text{OH}^*$	2.11 e12	0.0	480
21)	$\text{H}^* + \text{NO}_2^*$	$\rightleftharpoons \text{NO}^* + \text{OH}^*$	3.47 e14	0.0	1480
22)	$\text{H}_2 + \text{OH}^*$	$\rightleftharpoons \text{H}_2\text{O} + \text{H}^*$	2.16 e08	1.5	3430

$$k = AT^b e^{-Ea/T}$$



Mechanism for Ammonium-perchlorate / HTPB Reactions

